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$$\lim_{x \rightarrow 1} \frac{x^2 - 7x + 6}{1-x} = \frac{1-7+6}{1-1} = \frac{0}{0} \text{ (Ind)}$$

$$\lim_{x \rightarrow 1} \frac{(x-1)(x-6)}{1-x} = \lim_{x \rightarrow 1} -(x-6) = 5$$

$$\lim_{x \rightarrow 1} \frac{(x-1)^2}{1-x^2} = \frac{0}{0} \text{ (Ind)}$$

$$\lim_{x \rightarrow 1} \frac{-(x-1)^2}{(1-x)(1+x)} = \lim_{x \rightarrow 1} \frac{-(x-1)^2}{1+x} = \frac{0}{2} = 0$$

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c) $\lim_{x \rightarrow -1} \frac{x^3 + 4x^2 + 5x + 2}{x^2 - x - 2} = \frac{-1+4-5+2}{1+1-2} = \frac{0}{0} \text{ (Ind)}$

1	4	5	2
1	-1	-3	-2
0			

$$\lim_{x \rightarrow -1} \frac{(x+1)^2(x+2)}{(x+1)(x-2)} = 0$$

$$x = \frac{-3 \pm 1}{2} \begin{matrix} - \\ + \end{matrix}$$

d) $\lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h} = \frac{0}{0} \text{ (Ind)}$

$$\lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - x^2}{h} = \lim_{h \rightarrow 0} \frac{h(2x+h)}{h} = 2x$$

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14) $\lim_{x \rightarrow 2} \left(\frac{3}{\frac{x^2-5x+6}{(x-2)(x-3)}} - \frac{4}{x-2} \right) = \frac{3}{0} - \frac{4}{0} = \infty - \infty$

$$\lim_{x \rightarrow 2} \frac{3 - 4(x-3)}{(x-2)(x-3)} = \lim_{x \rightarrow 2} \frac{-4x+15}{(x-2)(x-3)} = \frac{7}{0} \text{ (Ind)}$$

$\lim_{x \rightarrow 2^-} f(x) = \frac{7}{0^+} = +\infty$ $\lim_{x \rightarrow 2^+} f(x) = \frac{7}{0^-} = -\infty$ \lim

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b) $\lim_{x \rightarrow 2} \frac{1-\sqrt{3-x}}{x-2} = \frac{1-1}{2-2} = \frac{0}{0} \text{ (Ind)}$

$$\lim_{x \rightarrow 2} \frac{(1-\sqrt{3-x})(1+\sqrt{3-x})}{(x-2)(1+\sqrt{3-x})}$$

$$\lim_{x \rightarrow 2} \frac{1-3+x}{(x-2)(1+\sqrt{3-x})} = \frac{1}{2}$$

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c) $\lim_{x \rightarrow 0} \frac{\sqrt{x+9}-3}{x^2} = \frac{0}{0}$ (Ind)

$\lim_{x \rightarrow 0} \frac{(\sqrt{x+9}-3)(\sqrt{x+9}+3)}{x^2(\sqrt{x+9}+3)}$

$\lim_{x \rightarrow 0} \frac{x+9-9}{x^2(\sqrt{x+9}+3)} = \lim_{x \rightarrow 0} \frac{1}{x(\sqrt{x+9}+3)} = \frac{1}{0}$

$\lim_{x \rightarrow 0^-} f(x) = \frac{1}{0^-} = -\infty$

$\lim_{x \rightarrow 0^+} f(x) = \frac{1}{0^+} = +\infty$

f.lim

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d) $\lim_{x \rightarrow 0} \frac{\sqrt{1+x}-\sqrt{1-x}}{3x} = \frac{0}{0}$ (Ind)

$\lim_{x \rightarrow 0} \frac{(\sqrt{1+x}-\sqrt{1-x})(\sqrt{1+x}+\sqrt{1-x})}{3x(\sqrt{1+x}+\sqrt{1-x})}$

$\lim_{x \rightarrow 0} \frac{1+x-1+x}{3x(\sqrt{1+x}+\sqrt{1-x})}$

$\lim_{x \rightarrow 0} \frac{2x}{3x(\sqrt{1+x}+\sqrt{1-x})} = \frac{0}{0}$

$\frac{2}{3(\sqrt{1+0}+\sqrt{1-0})} = \frac{1}{3}$

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$1^{\pm \infty}$

1.1 $\lim_{x \rightarrow a} \left(1 + \frac{1}{f(x)}\right)^{f(x)} = e$

1.2 $\lim_{x \rightarrow a} f(x)^{g(x)} = e^{\lim_{x \rightarrow a} g(x)(f(x)-1)}$

$\lim_{x \rightarrow 2} \left(\frac{x+2}{2x}\right)^{\frac{1}{2-x}} = \left(\frac{4}{4}\right)^{\frac{1}{0}} = 1^{\pm \infty}$ (Ind)

$e^{\lim_{x \rightarrow 2} \frac{1}{2-x} \left(\frac{x+2}{2x} - 1\right)}$

$e^{\lim_{x \rightarrow 2} \frac{1}{2-x} \frac{x+2-2x}{2x}} = e^{\lim_{x \rightarrow 2} \frac{1}{2-x} \frac{x+2-2x}{2x}} = e^{\lim_{x \rightarrow 2} \frac{1}{2-x} \frac{1}{2}} = e^{\frac{1}{2}} = \sqrt{e}$

$\lim_{x \rightarrow 1} \left(\frac{2x+1}{x}\right)^{\frac{1}{1-x}} = 3^{\frac{1}{0}}$

$\lim_{x \rightarrow 1^-} f(x) = 3^{\frac{1}{0^+}} = 3^{+\infty} = +\infty$

$\lim_{x \rightarrow 1^+} f(x) = 3^{\frac{1}{0^-}} = 3^{-\infty} = 0$

f.lim

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